

# A short introduction to SageMath

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**École de Physique des Houches**  
11 July 2018

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## The mission

*Create a viable free open source alternative to Magma, Maple, Mathematica and Matlab.*

# Some advantages of SageMath

## SageMath is free (GPL v2)

Freedom means

- 1 everybody can use it, by downloading the software from <http://sagemath.org>
- 2 everybody can examine the source code and improve it



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- no need to learn any specific syntax to use it
- easy access for students
- Python is a very powerful *object oriented language*, with a neat syntax

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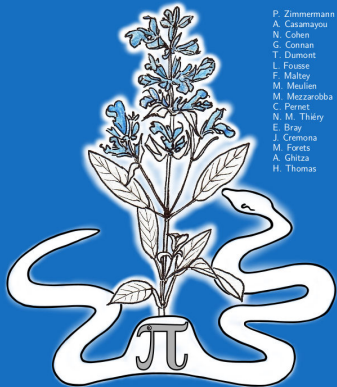
## SageMath is developing and spreading fast

...sustained by an enthusiastic community of developers



## Computational Mathematics with SageMath

P. Zimmermann  
A. Casamayou  
N. Cohen  
G. Connan  
T. Dumont  
L. Fousse  
F. Maltey  
M. Meulien  
M. Mezzarobba  
C. Pernet  
N. M. Thiéry  
E. Bray  
J. Cremona  
M. Forets  
A. Ghitza  
H. Thomas



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G. Connan, T. Dumont, L. Fousse, F. Maltey,  
M. Meulien, M. Mezzarobba, C. Pernet,  
N.M. Thiéry, E. Bray, J. Cremona, M. Forets,  
A. Ghitza & H. Thomas (2018)

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Freely downloadable from

[http:](http://sagebook.gforge.inria.fr/english.html)

[//sagebook.gforge.inria.fr/english.html](http://sagebook.gforge.inria.fr/english.html)

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MAKE='make -j8' make
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- **Run on your computer without installation: Sage Debian Live**  
<http://sagedebianlive.metelu.net/>  
Bootable USB flash drive with SageMath (boosted with octave, scilab),  
Geogebra, LaTeX, gimp, vlc, LibreOffice,...

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- **Open a (free) account on CoCalc** (formerly *SageMathCloud*)  
<https://cocalc.com/>
- **Run in SageMathCell**  
Single cell mode: <http://sagecell.sagemath.org/>

## Example 1: installing on Ubuntu 16.04 or 18.04

- 1 Download the archive `sage-8.2-Ubuntu_16.04-x86_64.tar.bz2` from one of the mirrors listed at <http://www.sagemath.org/download-linux.html>
- 2 Run the following commands in a terminal:

```
bunzip2 sage-8.2-Ubuntu_16.04-x86_64.tar.bz2
tar xvf sage-8.2-Ubuntu_16.04-x86_64.tar
cd SageMath
./sage -n jupyter
```

A Jupyter home page should then open in your browser. Click on *New* and select *SageMath 8.2* to open a Jupyter notebook with a SageMath kernel.

*NB:* **Ubuntu packages** are available for Ubuntu 18.04 (from the package manager, install `sagemath` and `sagemath-jupyter`). However, they are only for SageMath 8.1, so download the `tar.bz2` binaries instead to get the latest stable version (8.2).

## Example 2: using CoCalc

- 1 Open a free account on <https://cocalc.com/>
- 2 Create a new project
- 3 In the second top menu, click on *New* to create a new file
- 4 Select *Jupyter Notebook* for the file type

## Example 3: using SageMathCell

Simply open <http://sagecell.sagemath.org/>

# Various ways to run SageMath

- **Console mode:**

run `sage`

- **Jupyter Notebook:**

run `sage -n jupyter`

⇒ worksheet file format: `ipynb`

- **Legacy Sage Notebook:**

run `sage -n sagenb`

⇒ worksheet file format: `sws`

- **<https://cocalc.com/>:**

in your browser, open <https://cocalc.com/>

⇒ worksheet file format: `sagews`, `ipynb`

# Object-oriented notation in Python

As an **object-oriented language**, Python (and hence SageMath) makes use of the following **postfix notation** (same in C++, Java, etc.):

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result = object.function(arguments)
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In a **procedural language**, this would be written as

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## Examples

1. `riem = g.riemann()`
2. `lie_t_v = t.lie_der(v)`

NB: no argument in example 1

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- SageMath is still based on **Python 2.7**; heavy work is currently under way to migrate to **Python 3**.
- User commands are **preparsed** before being transmitted to the Python interpreter. In particular, this allows for standard mathematical notations, e.g.  $x^2$  instead of `x**2` (recall that `^` is the bitwise exclusive or (XOR) in Python).

To know what the preparsing is doing with the command `command`, run `preparse("command")`

# Let us try it!

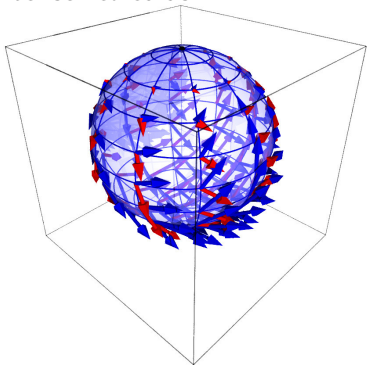
- First contact with SageMath:  
[http://nbviewer.jupyter.org/urls/gitlab.obspm.fr/gourgoul/SageMathTour/raw/master/Notebooks/first\\_contact.ipynb](http://nbviewer.jupyter.org/urls/gitlab.obspm.fr/gourgoul/SageMathTour/raw/master/Notebooks/first_contact.ipynb)
- 2D plots:  
[http://nbviewer.jupyter.org/urls/gitlab.obspm.fr/gourgoul/SageMathTour/raw/master/Notebooks/plot\\_tour\\_2D.ipynb](http://nbviewer.jupyter.org/urls/gitlab.obspm.fr/gourgoul/SageMathTour/raw/master/Notebooks/plot_tour_2D.ipynb)
- 3D plots:  
[http://nbviewer.jupyter.org/urls/gitlab.obspm.fr/gourgoul/SageMathTour/raw/master/Notebooks/plot\\_tour\\_3D.ipynb](http://nbviewer.jupyter.org/urls/gitlab.obspm.fr/gourgoul/SageMathTour/raw/master/Notebooks/plot_tour_3D.ipynb)
- Solving equations:  
[http://nbviewer.jupyter.org/urls/gitlab.obspm.fr/gourgoul/SageMathTour/raw/master/Notebooks/solve\\_tour.ipynb](http://nbviewer.jupyter.org/urls/gitlab.obspm.fr/gourgoul/SageMathTour/raw/master/Notebooks/solve_tour.ipynb)
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Download all notebooks at once:

```
git clone https://gitlab.obspm.fr/gourgoul/SageMathTour.git
```

# Tensor calculus with SageMath

**SageManifolds project:** extends SageMath towards **differential geometry** and **tensor calculus**



Stereographic-coordinates frame on  $\mathbb{S}^2$

- <http://sagemanifolds.obspm.fr>
- fully included in SageMath
- a dozen of contributors (developers and reviewers)  
cf. <http://sagemanifolds.obspm.fr/authors.html>
- want to stay tuned: subscribe to the **mailing list**
- help: <https://ask.sagemath.org>

Everybody is very welcome to contribute:  
visit <https://sagemanifolds.obspm.fr/contrib.html>