

# Errata

of the book

## SPECIAL RELATIVITY

### IN GENERAL FRAMES

<https://relativite.obspm.fr/sperel/>

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- p. 88, the right-hand side of Eq. (3.57) has the wrong sign; this equation should read

$$\underline{\Omega}_{\text{FW}} = ca(\underline{e}_0 \otimes \underline{e}_1 - \underline{e}_1 \otimes \underline{e}_0)$$

- p. 111, in the title of Sec. 4.5.2, replace *Secondw* by *Second*.
- p. 113, first line below Eq. (4.53): replace *The last two terms* by *The first two terms*.
- p. 113, first line below Eq. (4.55): replace *and the term  $2\vec{\omega} \times_u \vec{V}$*  by *and minus the term  $2\vec{\omega} \times_u \vec{V}$* .
- p. 117, first line below Eq. (4.66): replace *On the other side* by *On the other hand*
- p. 124, first line: replace  $V_{\text{light}} = c_{\odot} - V_{\oplus}$  by  $V_{\text{light}} = c_{\odot} + V_{\oplus}$ ; in the line below, replace  $V_{\text{light}} = c_{\odot} + V_{\oplus}$  by  $V_{\text{light}} = c_{\odot} - V_{\oplus}$ .
- p. 148, Sec. 5.5.1, 2nd paragraph, 4th line: replace  $t_1^{\text{rec}}, t_2^{\text{rec}}, t_1^{\text{em}}$  and  $t_2^{\text{em}}$  by  $t_1^{\text{em}}, t_2^{\text{em}}, t_1^{\text{rec}}$  and  $t_2^{\text{rec}}$ .
- p. 152, 3 lines below Eq. (5.66): replace  $f_1 f_2 = (1 - V^2) f_0^2$  by  $f_1 f_2 = (1 - V^2/c^2) f_0^2$ .
- p. 190, last paragraph, 2nd line: replace  $\vec{\ell}$  and  $\vec{k}$  are timelike by  $\vec{\ell}$  and  $\vec{k}$  are null.

- pp. 204 - 210: replace all occurrences of *Chap. 4* in Sec. 6.7 by *Chap. 5*.
- p. 210, 3rd line from the bottom: replace  $U' = V_1$  by  $U = V_1$ .
- p. 210, last line: replace  $-V_2 \sin \theta \vec{e}_2$  by  $V_2 \sin \theta \vec{e}_2$ .
- p. 214, first line above Eq. (6.117): a factor 2 is missing in the right-hand of the inline equation; it should read  $1 + \cosh \psi = 2 \cosh^2(\psi/2)$ .
- p. 215, Eq. (6.122): the last term in the numerator should be  $-\Gamma_2^2$ , so that the whole equation should read

$$\sin \theta = \left[ \frac{1 + 2\Gamma_1\Gamma_2 - \Gamma^2 - \Gamma_1^2 - \Gamma_2^2}{(\Gamma_1^2 - 1)(\Gamma_2^2 - 1)} \right]^{1/2}.$$

- p. 218, footnote 3: change the end of the first sentence to *of open sets such that any open set can be written as the (possibly infinite) union of some members of this family*.
- p. 220, 5 lines below Eq. (7.1): replace  $2\pi - \varphi_1$  by  $2\pi - \phi_1$ .
- p. 235, the middle equation in the system (7.44) has a spurious minus sign in its right-hand side; this equation should read

$$[\mathbf{K}_i, \mathbf{J}_j] = \sum_{k=1}^3 \epsilon_{ijk} \mathbf{K}_k$$

- p. 236, all the equations in the second and third lines of the system (7.45) have a spurious minus sign in their right-hand sides; these equations should read

$$\begin{aligned} [\mathbf{K}_1, \mathbf{J}_2] &= \mathbf{K}_3, & [\mathbf{K}_2, \mathbf{J}_3] &= \mathbf{K}_1, & [\mathbf{K}_3, \mathbf{J}_1] &= \mathbf{K}_2 \\ [\mathbf{J}_1, \mathbf{K}_2] &= \mathbf{K}_3, & [\mathbf{J}_2, \mathbf{K}_3] &= \mathbf{K}_1, & [\mathbf{J}_3, \mathbf{K}_1] &= \mathbf{K}_2 \end{aligned}$$

- p. 236, in the two lines above Eq. (7.46), the parts  $= -\mathbf{K}_2$  and  $= \mathbf{K}_1$  must be changed to respectively  $= \mathbf{K}_2$  and  $= -\mathbf{K}_1$ , so that these two lines becomes  
*Since from (7.45),  $[\mathbf{K}_1, \mathbf{K}_2] = -\mathbf{J}_3$ ,  $[\mathbf{K}_1, [\mathbf{K}_1, \mathbf{K}_2]] = -[\mathbf{K}_1, \mathbf{J}_3] = \mathbf{K}_2$  and  $[\mathbf{K}_2, [\mathbf{K}_1, \mathbf{K}_2]] = -[\mathbf{K}_2, \mathbf{J}_3] = -\mathbf{K}_1$ , (7.41) leads to.*
- p. 236, the signs in front of the  $1/12$  terms in Eq. (7.46) are wrong; this equation should read

$$\Lambda_1 \circ \Lambda_2 = \exp \left( \psi_1 \mathbf{K}_1 + \psi_2 \mathbf{K}_2 - \frac{1}{2} \psi_1 \psi_2 \mathbf{J}_3 + \frac{1}{12} \psi_1^2 \psi_2 \mathbf{K}_2 + \frac{1}{12} \psi_1 \psi_2^2 \mathbf{K}_1 + \dots \right)$$

- p. 244, first line below Eq. (7.71): replace  $-i$  by  $+i$  in the expression of  $\beta$ .
- p. 245, first line of footnote 11: replace 1927 by 1827.
- p. 247, unnumbered equation between Eqs. (7.81) and (7.82): replace  $(n^2)^3$  by  $(n^2)^2$ .
- p. 251, footnote 12: replace *same letters than* by *same letters as*.
- p. 266, 2 lines below Eq. (8.25): replace *Annexe A* by *Appendix A*.
- p. 268, 4 lines below Eq. (8.33): replace  $\text{Vect}(\vec{e}_0, \vec{e}_i)$  by  $\text{Span}(\vec{e}_0, \vec{e}_i)$ , as well as in the line below.
- p. 269: the last but one equation in the system (8.38) has a spurious minus sign in its right-hand side; this equation should read

$$[\mathbf{K}_i, \mathbf{J}_j] = \sum_{k=1}^3 \epsilon_{ijk} \mathbf{K}_k$$

- p. 296, Eq. (9.59):  $\vec{e}_x$  must be replaced by  $\underline{e}_x$ , so that the equation should read
 
$$\mathbf{p}_1 = \frac{E_1}{c} \underline{\mathbf{u}}_0 + P_1 \underline{\mathbf{e}}_x \quad \text{and} \quad \mathbf{p}_2 = m_2 c \underline{\mathbf{u}}_0$$
- p. 300, last line of Remark 9.14: replace “*bounces*” onto by “*bounces*” off.
- p. 307, immediately below Eq. (9.89): insert *Additional constraints, arising from other conservation laws, may forbid reaction (9.88):*.
- p. 315, Eq. (9.115):  $\underline{\mathbf{a}}_0$  must be replaced by  $\vec{\mathbf{a}}_0$  and  $m \frac{d\Gamma}{dt}$  by  $\frac{d}{dt}(\Gamma m)$ , as well as in the two unnumbered equations above Eq. (9.115).
- p. 338, first line above Eq. (10.61): replace  $V_{\parallel}^2 < c^2 - \vec{\mathbf{V}}_{\perp} \cdot \vec{\mathbf{V}}_{\perp}$  by  $V_{\parallel}^2(\vec{\sigma} \cdot \vec{\sigma}) < c^2 - \vec{\mathbf{V}}_{\perp} \cdot \vec{\mathbf{V}}_{\perp}$ .
- p. 338, third line of the paragraph starting by *Let us suppose*: replace *rayon* by *radius*.
- p. 338, fifth line above Eq. (10.62): insert *line* after *straight*.
- p. 340, second line of Sec. 10.6.2: replace *measured by to an* by *measured by an*.
- p. 345, first line below Eq. (10.78): replace *two vectors de* by *two vectors of*.
- p. 360, Remark 11.7: replace  $|h_{\alpha\beta}| \ll |g_{\alpha\beta}|$  by  $|(q/m)h_{\alpha\beta}| \ll |g_{\alpha\beta}|$ .

- p. 375, second line below Eq. (11.99): replace  $\mathbb{R}^4$  by  $\mathbb{R}^{16}$ .
- p. 376, end of Sec. 11.5.1.1: replace the last sentence by *Note that both sheets of the null cone, past and future, contribute to the action.*
- p. 376, fourth line below Eq. (11.101): replace *propagates thus* by *thus propagates*.
- p. 385, second line below Eq. (12.13): replace *in the proper time* by *is the proper time*.
- p. 405, second unnumbered equation at the top of the page: replace  $y'_*$  by  $y_*$  and  $z'_*$  by  $z_*$ .
- p. 414, Eq. (12.85): remove the factor  $1/2$  in front of  $V^2/c^2$ .
- p. 415, first line below Eq. (12.89): replace  $mc^2 + b$  by  $m(c^2 + \gamma b)$ .
- p. 420, Table 12.1: in the first row, replace  $\Lambda_0$  by  $\Lambda$  and, in the last row, replace  $\vec{\epsilon}_1$  by  $\vec{\epsilon}$ .
- p. 435, first line below Eq. (13.23): replace *has not exactly* by *does not have exactly*.
- p. 445, last line of footnote 4: replace *not less* by *no less*.
- p. 446, 6th line above Eq. (13.49): replace *Even, we shall use* by *We shall even use*.
- p. 446, last but one line: replace  $\vec{u} \cdot d\vec{V} = 0$  by  $\vec{u} \cdot \vec{V} = 0$ .
- p. 465, third line below Eq. (13.103b): replace *the same than that at the emission* by *the same as the one during the emission*
- p. 467, unnumbered equation above Eq. (13.108): the expression of  $v_-$  should be  $c + r\omega$ , so that the whole equation becomes
 
$$v_+ = c - r\omega \quad \text{and} \quad v_- = c + r\omega \quad (\text{aether})$$
- p. 467, last but one line: replace *This is thus Georges Sagnac* by *It is thus Georges Sagnac*.
- p. 493, fourth line above Eq. (14.80): replace *We recognize in the first term* by *We recognize in the first two terms* and, two lines below, replace *second term* by *third term*.
- p. 495, third line above Eq. (15.1): replace *pure mathematical* by *purely mathematical*.

- p. 498, third line of Remark 15.1: replace *We had not to use* by *We did not have to use*.
- p. 521, Eq. (16.1): replace the wedge product by a cross product, so that the equation becomes:

$$dV = d\vec{\ell}_1 \cdot (d\vec{\ell}_2 \times d\vec{\ell}_3).$$

- p. 724, first line of legend of Fig. 22.3: replace *on a polar orbit* by *in a polar orbit*.
- p. 724, second line of Sec 22.3.2: replace *leads to abandon* by *leads to the abandoning of*
- p. 725, 6th line below Eq. (22.30): replace *leads to abandon* by *leads to the abandoning of*